$10 \times 2 = 20$

Attempt ALL questions. Each question carries 2 marks.

1.

4.

(-4, -3).

Find the equation of the sphere passing through (0, 0, 0), (a, 0, 0), (0, b, 0). 2. (0,0,c).Find the equation of the parabola whose focus is (3, 1) and vertex is (3, -2). 3.

Find the equation of the circle passing through the origin and has centre at

Find the equation of the parabola whose focus is
$$(3, 1)$$
 and vertex is $(3, -2)$.

One focus of a hyperbola is located at the point $(1, -3)$ and the corresponding

directix is the line y = 2. Find the equation of the hyperbola if its eccentricity is $\frac{3}{2}$. If $y = ax^2 + 3b/x$ then show that $x^2 y_2 = 2y$. 5. Evaluate $\int \cot^2 x \, dx$. 6.

7. Evaluate
$$\int_{2}^{2} x e^{x} dx$$
.
8. Evaluate $\int_{2}^{2} \sqrt{4-x^{2}} dx$.

State the trapezoidal rule for numerical integration of a function f(x) over the 9. interval [a, b] by dividing [a, b] into n subintervals. **10.** Solve $\frac{dy}{dx} = \frac{x - y + 2}{x + y - 1}$.

11. Find the equation of the circle passing through (1, 1), (2, -1), (3, 2). 12. Find the equation of the parabola whose focus is (3, -2) and directrix is

3x + 2y - 4 = 0. 13. Find the centre, eccentricity, vertices, foci and the equations of directrices of the ellipse $x^2 + 2y^2 - 4x + 12y + 14 = 0$.